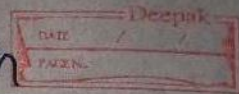


Simple Harmonic Motion



Simple harmonic motion



Periodic Motion → Motion which repeats itself after equal interval of time.

T = time period of periodic motion.



Some example of periodic motion

1. Motion of earth around sun.
 2. Uniform Circular motion
 3. Satellite motion.
 4. An insect is climbing on wall & fall in equal interval.
 5. Ball is bouncing b/w two fixed point (ground and roof)
 6. Simple pendulum (No damping)
 7. Spring mass system.
- All periodic are not oscillatory.

Oscillation :-

Periodic motion which is to & fro

- All oscillatory are periodic
- Oscillation or Vibration motion is defined as a periodic and bounded motion of a body

→ Vibration - High frequency

SHM (Simple harmonic motion)

Oscillation with small amplitude.



Periodic

Motion repeats its path in
Fixed Interval

About mean position

To & fro
(Oscillation)

Not about any
mean

Non-oscillatory

Ex: Circular motⁿ
Satellite motion

Amplitude large
(Variable)

Amplitude small
(Energy conserved)

- Not simple harmonic
motion

Amplitude - fixed
restoring force
S.H.M.

Ques Periodic motion must be oscillatory motion $\rightarrow$ False

2. Periodic motion may be oscillatory motion $\rightarrow$ True

3. Oscillatory motion must be periodic $\rightarrow$ True

4. S.H.M must be periodic & oscillatory $\rightarrow$ True

5. Oscillation must be simple harmonic $\rightarrow$ False

6. Oscillation may be simple harmonic $\rightarrow$ True

Variable amplitude $\rightarrow$

Not a periodic

Ques Circular motion is an example of:

- (a) Periodic motion
- (b) Non periodic
- (c) Oscillatory
- (d) may be periodic or non periodic ✓

Ques The circular motion of a particle with const speed is

- (1) Periodic but not Simple harmonic ✓
- 2 Simple harmonic but not periodic
- 3 Period and simple harmonic
- 4 Neither periodic nor simple harmonic

Period and frequency

Period is the interval of time after which the motion is repeated. It is denoted by T

— frequency is defined as the num. of oscillations per unit time. It is the reciprocal of time period T . It is represented by the symbol

The relation b/w ω and T is

$$f = \nu = \frac{1}{T}$$

$$\omega = 2\pi f$$

$$\omega = \frac{2\pi}{T} \frac{\text{rad}}{\text{sec}}$$

Angular freq. = Angular Speed.

Time Period.

$$T = \frac{2\pi}{\omega} = 2\pi \sqrt{\frac{m}{k}}$$

Q. If frequency of Object is π rad/sec then find time period.

$$\omega = \pi \text{ rad/sec} = \frac{2\pi}{T}$$

$$T = 2 \text{ sec}$$

Q. A nurse in a hospital noted for a patient the heart was beating 75 times a minute find its frequency and time period.

75 Hm in a minute (60 sec)

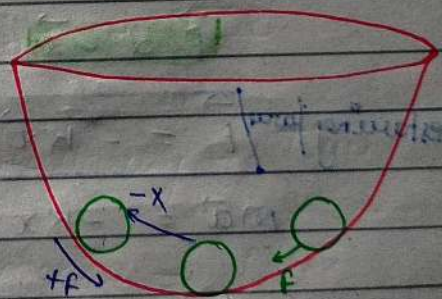
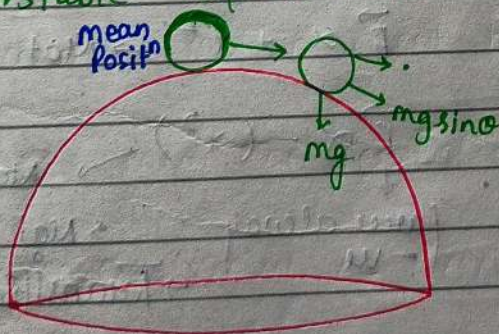
$$60 \text{ sec} \quad \frac{75}{60} \text{ in}$$

$$1 \text{ sec} \quad \frac{75}{160}$$

$$f = 1.25 \text{ Hz}$$

$$T = \frac{1}{1.25} \text{ sec} = 0.8 \text{ sec}$$

Unstable equilibrium.

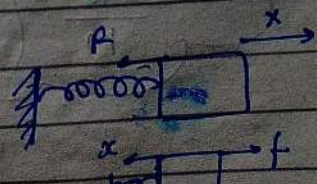
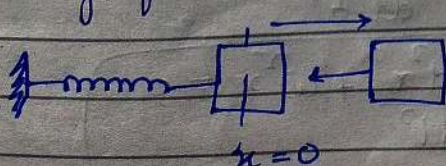


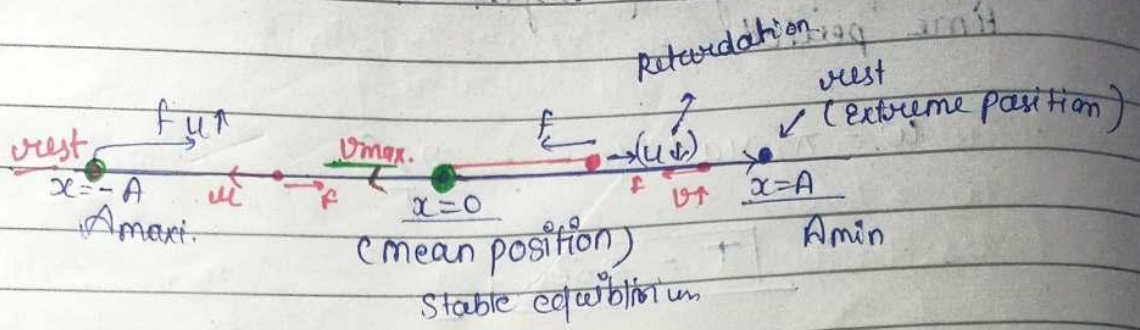
Stable equilibrium.

Oscillation

SHM (Small amplitude)

Restoring force oppose motion $\rightarrow F$

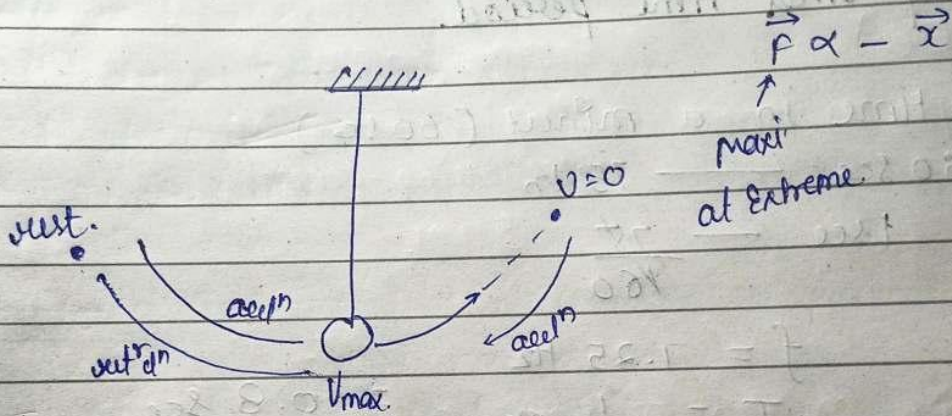




Restoring force always acts towards mean position

$$F_{net} = 0$$

$$a_{ce} = 0$$



Condition of SHM

$$\vec{F} \propto -\vec{x}$$

Restoring force $\vec{F} = -K\vec{x}$

$$m\vec{a} = -K\vec{x}$$

$$\vec{a} = \frac{-K}{m} \vec{x}$$

$$\vec{a} = -\omega^2 \vec{x}$$

$$\omega^2 = \frac{K}{m} = \left(\frac{2\pi}{T}\right)^2$$

$$\vec{F} \propto +x^2 \rightarrow \text{Not SHM}$$

$$\vec{F} \propto -(x^2)$$

force always $\rightarrow$ No SHM

$\rightarrow$ Nat Oscillⁿ

$\rightarrow$ Transitional motion

accelⁿ ka double diff.

$$\frac{d^2\vec{x}}{dt^2} = -\omega^2 \vec{x}$$

$$\frac{d^2\vec{x}}{dt^2} + \omega^2 \vec{x} = 0$$

* differential form of SHM.

$F = -x^3$ — Oscillation but not S.H.M.

$F = -x^n \rightarrow n = 0, 2, 4, 6, 8$ even no
— only transitional

Ans
 $\rightarrow n = 1 \rightarrow$ S.H.M

$\rightarrow n = 1, 3, 5, 7 \rightarrow$ Oscillation not S.H.M.

Ques main

If force $F = -4x + 8$ then due to this force motion

(a) Oscillation but not Periodic

✓ (b) SHM with equilibrium at $2m$

(c) " " " " $\frac{1}{2}m$

(d) Oscillation but not S.H.M

soln

$F \propto -x$

$$F = 0 = -4x + 8$$

$$4x = 8 \Rightarrow x = \frac{8}{4} = \boxed{x = 2m}$$

Ques A particle move under force $F = -5(x-2)^3$ motion of the particle is.

$$F = -5(x-2)^3$$

① Translatory

② Oscillatory ✓

③ S.H.M

④ All of these

$$x = -4$$

$$F = +ve.$$

Ques For a particle showing motion under the force $F = -5(x-2)^2$, the motion is.

① Translatory =

② Oscillatory

③ SHM

$$F = -5(x-2)^2 \propto \text{even no.}$$

Q1 A particle moves under force $F = -5(x-2)^3$. motion of the particle is.

- ① Translatory
- ② Oscillatory ✓
- ③ SHM
- ④ All of these

Q2 If a particle is executing simple harmonic motion, then acceleration of particle

- ① Is uniform
- ② Varies linearly with time
- ③ Is not uniform ✓
- ④ Both 2, 3

Q3 A particle moves such that acceleration is given by $a = -4x$, the period of oscillation is

① x ✓

② $2/\pi$

③ $1/\pi$

④ 2π ✓

$$a = -4x$$

$$a = -\omega^2 x$$

$$\omega^2 = 4$$

$$\omega = \sqrt{4} = 2$$

$$\frac{2\pi}{T} = 2$$

$$T = 2\pi$$

Condition of SHM

$$\vec{F} \propto -\vec{x}$$

$$\vec{F} = -K\vec{x}$$

$$\vec{a} = -\frac{K}{m}\vec{x}$$

$$a = -\omega^2 x$$

$$\frac{d^2x}{dt^2} = -\omega^2 x$$

$$\frac{d^2x}{dt^2} + \omega^2 x = 0$$

$$x \propto t^2$$

$$x \propto t$$

$$x \propto -t$$

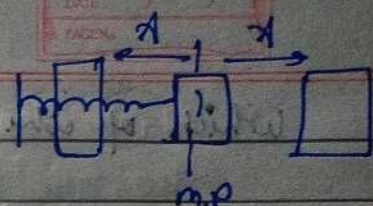
$$x \propto (t^2)$$

Relation
b/w position
& time

$$\frac{d^2x}{dt^2} + \omega^2 x = 0$$

$$x = A \sin(\omega t + \phi)$$

Position of particle at time 't'



A = Amplitude - Max^m position from mean position

ϕ = Initial phase diff (at $t=0$)

decide from where motion has started

ω = Angular frequency

Q find value of ϕ if motⁿ started

$$t=0, x=0$$

$$0 = A \sin(0 + \phi)$$

$$0 = \sin \phi \quad (\phi = 0^\circ)$$

Q If motion started from the Extreme then find ϕ

$$\phi/2 = 90^\circ$$

$$x = A \sin(\omega t + \phi)$$

$$x = A \sin(\omega t + \frac{\pi}{2}) = A \cos(\omega t)$$

Q If motion started from $x = +\frac{A}{2}$ find ϕ

$$\frac{\phi}{6} = 30^\circ$$

$$x = A \sin(\omega t + \frac{\phi}{6})$$

Q If motion started from $x = \frac{A}{\sqrt{2}}$ find ϕ

$$\frac{\phi}{4} = 45^\circ$$

$$x = A \sin(\omega t + \frac{\pi}{4})$$

Which of the following is are not SHM

$y = A \cos \omega t$ ✓

$y = A \sin \omega t$ ✓

$y = A \sin(3\omega t)$ ✓

$y = Ae^{kt}$ ✗

If motion started from mean position then find

Position / time

Velocity / time

accelⁿ / time

$\phi = 0$ (motion start from mean)

$x = A \sin(\omega t + \phi)$

$x = A \sin(\omega t)$

$\frac{dx}{dt} = v = A \cos(\omega t) \times \omega$

$v = A\omega \cos(\omega t)$

$a = \frac{dv}{dt} = -A\omega^2 \sin(\omega t)$

$a = -A\omega^2 \sin(\omega t)$

Imp $a = -\omega^2 x$

$$x = A \sin(\omega t)$$

$$V = \omega A \cos(\omega t)$$

$$a = -A\omega^2 \sin(\omega t)$$

$$a = -\omega^2 x$$

For mean

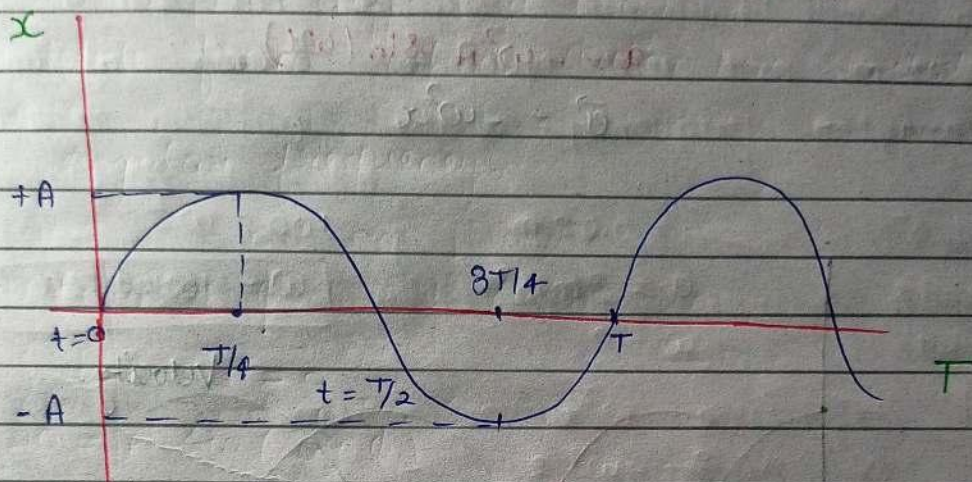
$$V = \omega \sqrt{A^2 - x^2}$$

$$x = A \sin(\omega t + \phi)$$

$$V = A\omega \cos(\omega t + \phi)$$

$$a = -A\omega^2 \sin(\omega t + \phi)$$

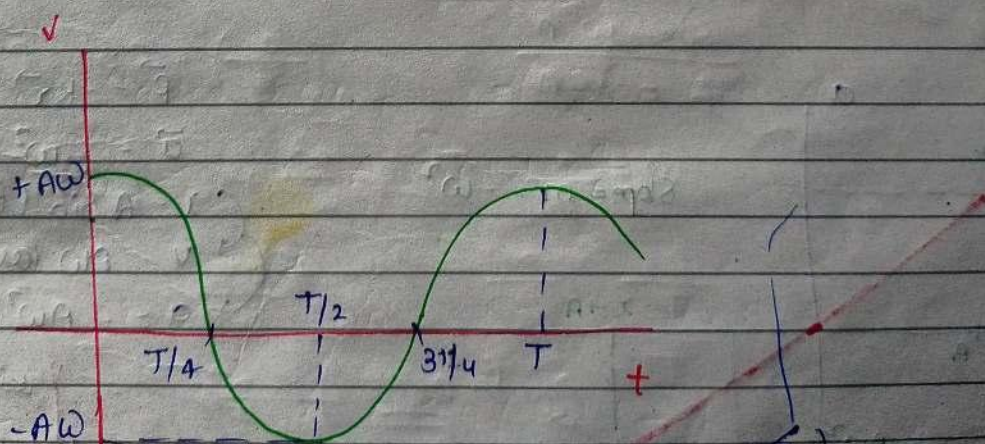
For general S.H.M



$$x = A \sin(\omega t)$$

$$x = A \sin\left(\frac{2\pi}{T} \times \frac{T}{2}\right)$$

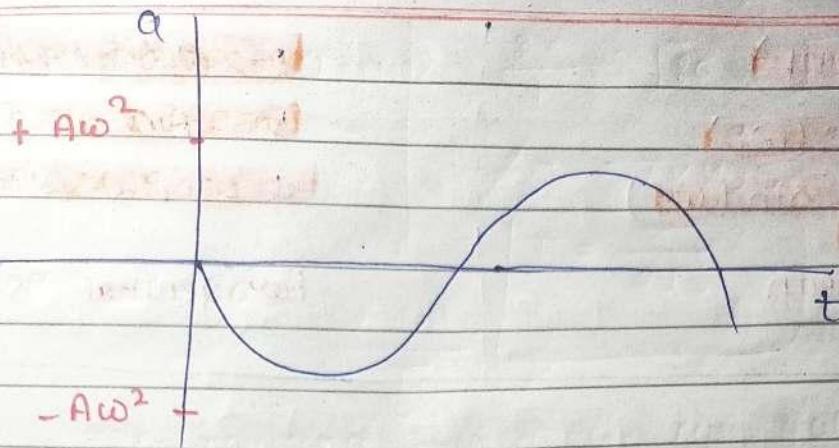
$$\text{at } t = \frac{T}{2}$$



$$V = A\omega \cos(\omega t) \rightarrow A\omega \cos\left(\frac{2\pi}{T} \times \frac{T}{2}\right)$$

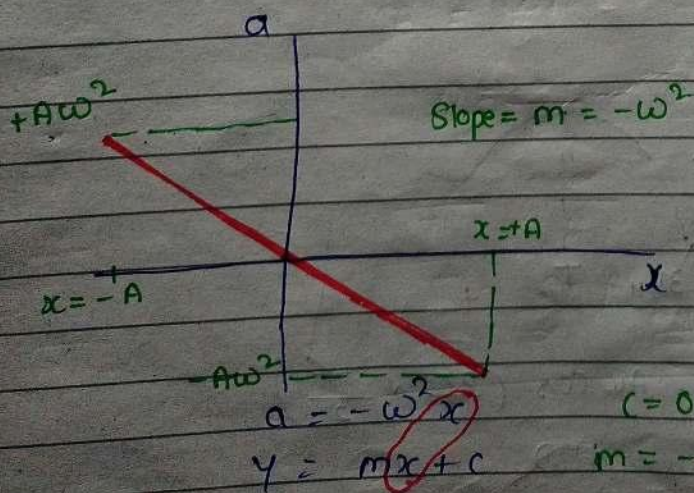
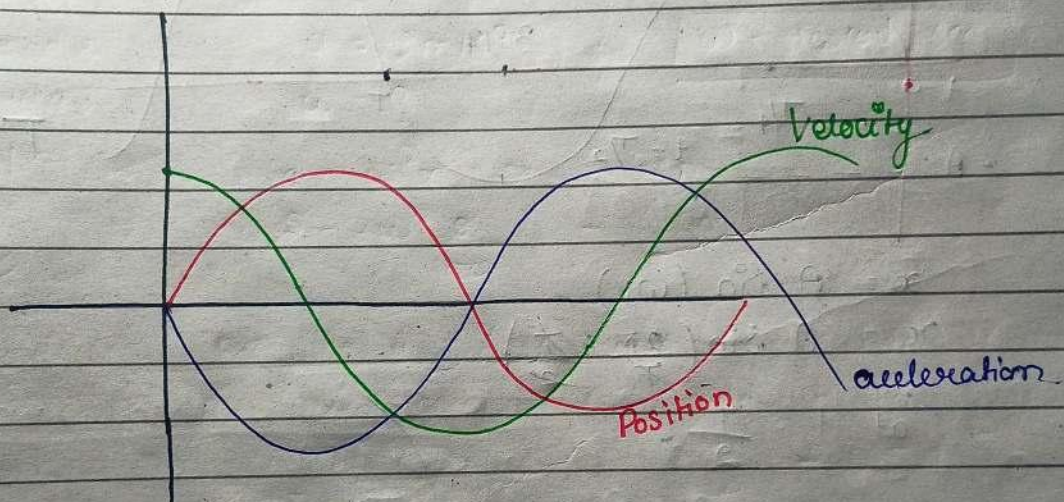
$$t = 0, \text{ mean, } V_{\max} = A\omega$$

$$t = \frac{T}{4}, \text{ extreme, } V = 0$$



$$a = -\omega^2 A \sin(\omega t)$$

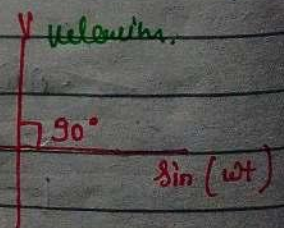
$$\vec{a} = -\omega^2 \vec{x}$$



$$\vec{F} = -K\vec{x}$$

$$\vec{a} = -\omega^2 \vec{x}$$

$$\begin{cases} x = A \sin(\omega t) \\ v = A\omega \cos(\omega t) \\ a = -A\omega^2 \sin(\omega t) \end{cases}$$



Position $\xrightarrow{\frac{\pi}{2}}$ Velocity $\xrightarrow{\frac{\pi}{2}}$ Acceleration
 v_0 $\frac{\pi}{2}$ Max $\frac{\pi}{2}$ $uske$

Ques 1 Phase diff b/w the Inst. Velo and accelⁿ of a particle executing S.H.M is

- ① zero ② $\frac{\pi}{2}$ ③ π ④ 2π

Ques 2 A particle executing SHM along y-axis, which is described by $y = 10 \sin \frac{\pi t}{4}$, phase of particle at $t = 2$ sec is.

① $\frac{\pi}{4}$

② $\frac{\pi}{2}$

③ $\frac{\pi}{8}$

$y = 10 \sin \left(\frac{\pi t}{4} \right)$
 Phase $= \frac{\pi t}{4} = \frac{\pi \times 2}{4} = \frac{\pi}{2}$

Ques 3 Two Simple Harmonic motion of angular frequency 100 and 1000 rad^{-1} have the same displacement amplitude. The ratio of their maxim^m accelⁿ.

$\omega_1 = 100$

$\omega_2 = 1000$

$\frac{a_{\max} = \omega_1^2 A}{a_m = \omega_2^2 A} = \left(\frac{10^2}{10^3} \right)^2 = \left(\frac{1}{10} \right)^2 = \frac{1}{10^2}$

Ques 4 A particle execute Simple Harmonic motion according to equation $4 \frac{d^2 x}{dt^2} + 320 x = 0$. Its Time period of Oscillation is.

① $\frac{2\pi}{5\sqrt{3}}$ s

② $\frac{\pi}{3\sqrt{2}}$ s

③ $\frac{\pi}{2\sqrt{3}}$ s

④ $\frac{2\pi}{\sqrt{3}}$ s

$$4a + 320\pi = 0$$

$$4a = -320\pi$$

$$a = -80\pi$$

$$\omega^2 = 80$$

$$\frac{2\pi}{T} = \sqrt{80} = \sqrt{16 \times 5}$$

$$2\pi = T \times 4\sqrt{5}$$

$$T = \frac{\pi}{2\sqrt{5}}$$

Ques 5 If a Simple harmonic Oscillator has got a displacement of 0.02 m and accelⁿ equal to 2.0 m/s^2 at any time. The angular frequency of the Oscillator is equal to

(a) 10 rad s^{-1}

$$x = 0.02 \text{ m}$$

$$100 = \omega^2$$

(b) 0.1 rad s^{-1}

$$a = 2 \text{ m/s}^2$$

$$\omega = 10 \text{ rad/sec}$$

(c) 100 rad s^{-1}

$$\omega = ?$$

(d) 1 rad s^{-1}

$$a = -\omega^2 x$$

$$2 = +\omega^2 \cdot \frac{2}{100}$$

40.

Ques 6 A particle is executing a Simple harmonic motion. Its maximum accelⁿ is α , maximum velocity is β . Then its Time period of vibration will be

(a) $2\pi\beta$

$$\frac{\alpha}{\beta} = \omega^2 A$$

(b) $\frac{\beta^2}{\alpha^2}$

$$\omega = \frac{\alpha}{\beta}$$

(c) $\frac{\alpha}{\beta}$

$$\frac{2\pi}{T} = \frac{\alpha}{\beta}$$

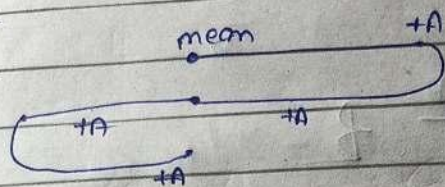
(d) $\frac{\alpha}{\beta^2}$

$$T = \frac{2\pi\beta}{\alpha}$$

(e) $\frac{\beta^2}{\alpha}$

Q7 The distance covered by a particle undergoing SHM in one time period is (amplitude = A)

- (a) $4A$ ✓
 (b) Zero
 (c) A
 (d) $2A$



displacement is oscillation $\neq 0$
 dist in one oscillation = $4A$

Q8 A particle is executing SHM with amplitude A and has maximum velocity V_0 . Its speed at displacement $\frac{3A}{4}$ will be
 Amplitude = A
 Velocity = V_0

(a) $\frac{\sqrt{7}}{4} V_0$

$x = \frac{3A}{4}$, $V_0 = A\omega$

(b) $\frac{V_0}{\sqrt{2}}$

$V = \omega \sqrt{A^2 - x^2}$

(c) V_0

$V = \omega \sqrt{A^2 - \frac{9A^2}{16}}$

(d) $\frac{\sqrt{3}}{2} V_0$

$\omega A \sqrt{\frac{16-9}{16}} = V_0 \sqrt{\frac{7}{16}} = \frac{\sqrt{7} V_0}{4}$

Q9 Which one of the following statement is true for the velocity V and the acceleration a of a particle executing simple harmonic motion?

- (1) When V is maximum, a is zero ✓
 (2) When V is zero, a is zero
 (3) When V is maximum, a is maximum
 (4) Value of a is zero, whatever may be the value of V



Ques 10 For a particle executing simple harmonic motion, the amplitude is A and the period is T .

- ① $4\pi T$
- ② $\frac{2A}{T}$
- ③ 2π
- ④ $\frac{2\pi A}{T}$

Ques 11 A body is executing S.H.M. when its displacement from the mean position is 4 cm and 5 cm, the corresponding velocity of the body is 10 cm/sec.

- ① 2π sec
- ② $\pi/2$
- ③ π
- ④ $3\pi/2$

$$x_1 = 4 \text{ cm}$$

$$x_2 = 5 \text{ cm}$$

$$v_1 = 10 \text{ cm/sec}$$

$$v_2 = 8 \text{ cm/sec}$$

$$\frac{10}{8} = \frac{\sqrt{A^2 - 16}}{\sqrt{A^2 - 25}} \Rightarrow \left(\frac{10}{8}\right)^2 = \frac{A^2 - 16}{A^2 - 25} \quad \text{--- (1)}$$

$$\frac{100}{64} = \frac{A^2 - 16}{A^2 - 25}$$

$$\frac{100}{64} = \frac{A^2 - 16}{A^2 - 25} \Rightarrow \left(\frac{10}{8}\right)^2 + 16 = A^2 \quad \text{--- (2)}$$

$$\left(\frac{10}{8}\right)^2 + 16 = \left(\frac{8}{8}\right)^2 + 25$$

$$\frac{100}{64} - \frac{64}{64} = 25 - 16$$

$$\frac{36}{64} = 9 = \omega^2 = 4$$

$$\frac{2\pi}{T} = 2$$

$$T = \pi$$

Q12 A body of mass 0.01 kg executes Simple Harmonic motion about $x=0$ under the influence of a force as shown in figure. The time period of SHM is

① 1.05 s

② 0.52 s

③ 0.25 s

④ 0.03 s

$$\vec{F} = -K\vec{x}$$

$$+80 = +K \cdot 0.2$$

$$K = \frac{80}{0.2} \times 10$$

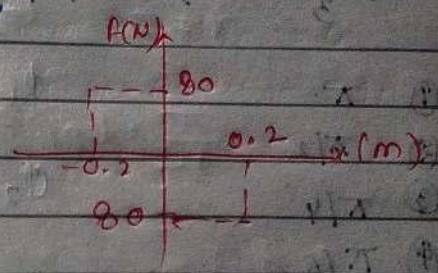
$$K = 400$$

$$m\omega^2 = 400$$

$$\frac{1}{100} \omega^2 = 400$$

$$\omega^2 = 400 \times 100, \quad \frac{\omega}{T} = 2 \times 10^2$$

$$T = \frac{\pi}{\frac{\omega}{T}} = \frac{3.14}{100} = 0.0314$$



Q13 A particle is executing SHM about $y=0$ along y -axis its position at an instant is given by $y(\text{m}) = 5(\sin 3\pi t + \sqrt{3} \cos 3\pi t)$. The amplitude of oscillation is

① 10 m

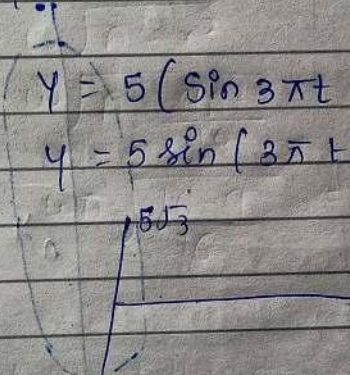
② 5 m

③ $5(1+\sqrt{3}) \text{ m}$

④ $5\sqrt{3} \text{ m}$

$$y = 5(\sin 3\pi t + \sqrt{3} \cos 3\pi t)$$

$$y = 5 \sin(3\pi t) + 5\sqrt{3} \cos(3\pi t)$$



$$\sqrt{25 + 25 \times 3}$$

$$\sqrt{100}$$

$$= 10$$

Q14 Particle executing SHM along y -axis has its motion described by the equation $y = 2 + 10 \sin 5\pi t$. Amplitude of SHM is.

① 2

② 12

③ 10

④ $\sqrt{104}$

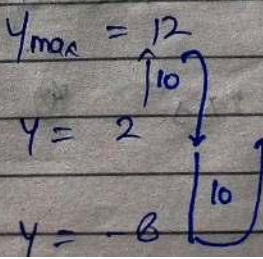
$$y = 2 + 10 \sin(5\pi t)$$

Amplitude = 0

$$y = 2 + 10(-1)$$

$$2 - 10$$

$$= -8$$



Ques 15

The displacement of two particles executing SHM on the same lines are given as $y_1 = a \sin(\frac{\pi}{2}t + \phi)$ and $y_2 = b \sin(\frac{2\pi}{3}t + \theta)$. The phase difference b/w them at $t=1s$

① π

② $\pi/2$

③ $\pi/4$

④ $\pi/6$

$$\phi_1 = \frac{\pi}{2} + 0$$

$$\phi_2 = \frac{2\pi}{3} + 0$$

$$\phi_2 - \phi_1 = \frac{2\pi}{3} - \frac{\pi}{2} = \frac{4\pi - 3\pi}{6} = \frac{\pi}{6}$$

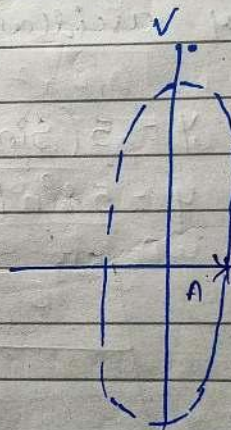
diff graph

$$V = \omega \sqrt{A^2 - x^2}$$

$$\frac{V}{\omega} = \sqrt{A^2 - x^2}$$

$$\frac{V^2}{\omega^2} = A^2 - x^2$$

$$\frac{V^2}{\omega^2} + x^2 = A^2$$



divided by A^2 both side

$$\frac{V^2}{\omega^2 A^2} + \frac{x^2}{A^2} = 1$$

Ques 16 The plot of velocity (v) versus displacement (x) of a particle executing simple harmonic motion is shown in figure. The time period of oscillation of particle is

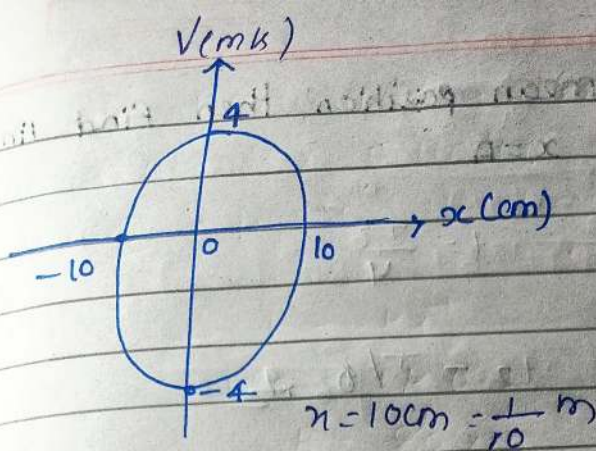
① $\frac{\pi}{2} s$

② $\frac{\pi}{20} s$

③ $2\pi s$

④ $3\pi s$





$$\omega r = 4$$

$$\frac{2\pi}{T} \cdot \frac{1}{10} = 4$$

$$T = \frac{\pi}{20}$$

Q. Graph Velocity and acceleration.

$$a = -\omega^2 x \quad \Rightarrow \quad \left(\frac{a}{\omega^2}\right)^2 = (-x)^2 \Rightarrow \frac{a^2}{\omega^2} = x^2 \quad \text{--- (i)}$$

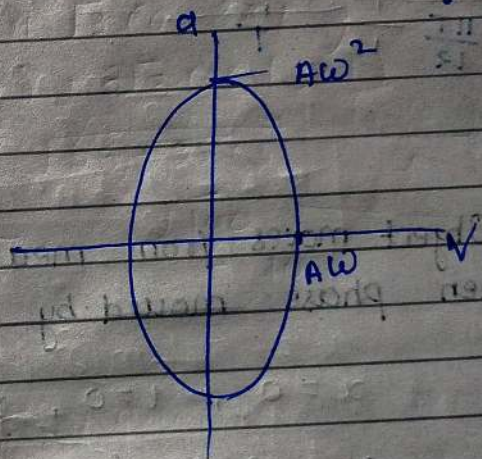
$$V = \omega \sqrt{A^2 - x^2}$$

$$\frac{V^2}{\omega^2} = A^2 - x^2 \quad \text{--- (ii)}$$

$$= \frac{a^2}{\omega^2} + \frac{V^2}{\omega^2} = x^2 + A^2 - x^2$$

$$\frac{a^2}{\omega^4} + \frac{V^2}{A^2 \omega^2} = 1$$

$$\frac{a^2}{(A\omega)^2} + \frac{V^2}{(A\omega)^2} = 1$$



Q. Motion start from mean position then find time taken from $x=0$ to $x=A/2$

$$x = A \sin(\omega t)$$

$$\frac{A}{2} = A \sin(\omega t)$$

$$\frac{1}{2} = \sin(\omega t)$$

$$\omega t = \frac{\pi}{6}$$

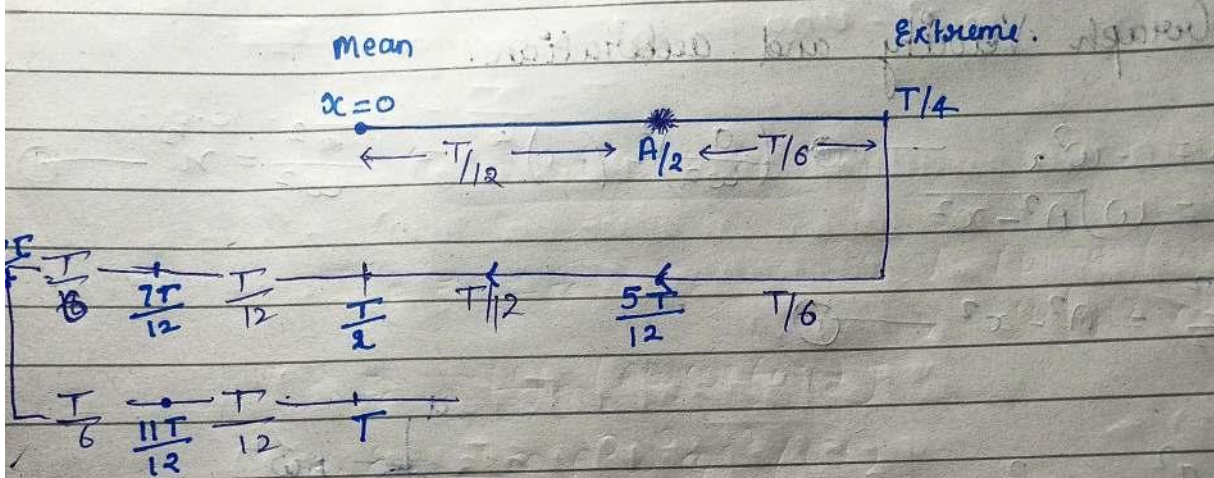
$$\frac{2\pi}{T} t = \frac{\pi}{6}$$

$$t = \frac{T}{12}$$

Q18 Motion start from mean position then find time taken from $x = \frac{A}{2}$ to $x = A$

$$x = 0 \text{ to } x = A \text{ — } t = \frac{T}{4}$$

$$\frac{T}{12} + t_2 = T/4, \quad t_2 = T/6 \text{ Ans.}$$



Q19 Object moves from mean half of the extreme ($x = \frac{A}{2}$) then phase moved by object at that time 't'

$$x = 0, \quad t = 0, \quad \phi = 0$$

$$x = A \sin(\omega t)$$

$$\frac{A}{2} = A \sin(\omega t)$$

$$\frac{1}{2} = \sin \omega t$$

$$\boxed{\omega t = \frac{\pi}{6}}$$

Ques 20 Find time taken from mean to $x = \frac{A}{\sqrt{2}}$

$$\phi = \frac{\pi}{4}$$

$$T = \frac{T}{8}$$

Ques 21 A particle is executing S.H.M b/w $x = \pm A$, the time taken to go from $\frac{A}{2}$ to $\frac{A}{2}$ is T_1 and to go from $\frac{A}{2}$ to A is T_2 then.

① $T_1 < T_2$ ✓

② $T_1 > T_2$

③ $T_1 = T_2$

④ $T_1 = 2T_2$

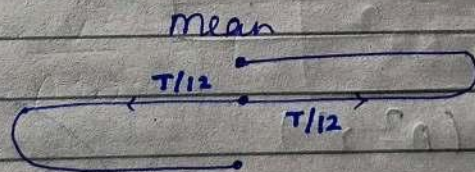
Ques 22 A particle is executing SHM with time period T . Starting from mean position, time taken by it to complete $\frac{5}{8}$ oscillation is.

① $\frac{T}{12}$

② $\frac{T}{6}$

③ $\frac{5T}{12}$

④ $\frac{7T}{12}$ ✓



$\frac{5}{8}$ oscillation

$$\frac{4+1}{8} = \frac{4}{8} + \frac{1}{8}$$

$$= \frac{1}{2} + \frac{1}{8}$$

$$= \frac{5}{8} T$$

$$T = \frac{T}{2} + \frac{T}{12}$$

$$\frac{6T + T}{12} = \frac{7T}{12}$$

Ques 23 Two particle executing SHM of same frequency meet at $x = +\frac{A}{2}$

$$\frac{x}{6}$$

$$\frac{x}{3}$$

$$\frac{5\pi}{6}$$

$$\frac{2\pi}{3}$$

$$x = A/2$$

$$\theta_1 = \frac{\pi}{6}$$

$$\theta_2 = \frac{5(2\pi)}{6} = \frac{5\pi}{6}$$

$$\Delta\phi = \frac{5\pi}{6} - \frac{\pi}{6}$$

Kinetic Energy

$$K.E = \frac{1}{2} mv^2$$

$$V = A\omega \cos(\omega t)$$

$$V = \omega \sqrt{A^2 - x^2}$$

$$K.E = \frac{1}{2} m (A\omega \cos(\omega t))^2$$

$$K.E = \frac{1}{2} m A^2 \omega^2 \cos^2(\omega t)$$

$$K.E = \frac{1}{2} K A^2 \cos^2(\omega t)$$

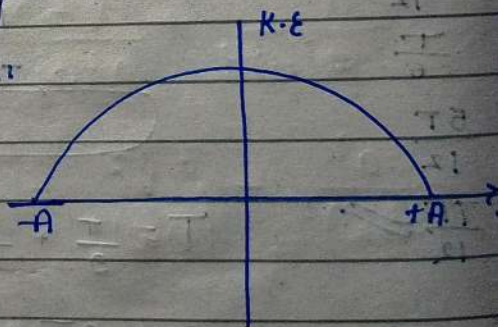
if it is zero

$$K.E = \frac{1}{2} m \omega^2 (A^2 - x^2)$$

$$K.E = \frac{1}{2} K (A^2 - x^2)$$

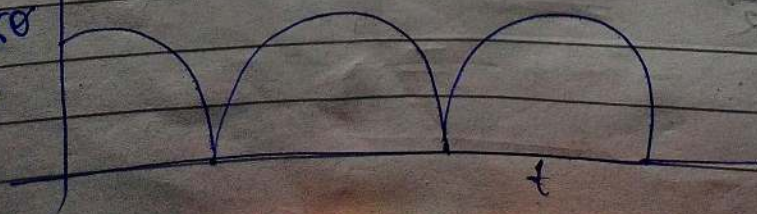
if $(x=A)$ at extreme $K.E = 0$

if $(x=0)$ at mean $K.E = \frac{1}{2} K A^2$



K.E

$\cos^2 \theta$



Potential Energy

$$\vec{F} = -k\vec{x}$$

ref at mean ($U_0 = 0$)

$$F \frac{du}{dx} = -kx$$

$$U = \frac{1}{2} kx^2$$

$$\int_{U_0}^U du = \int_{x=0 \text{ (mean)}}^x kx dx$$

$$U = \frac{1}{2} kA^2 \sin^2(\omega t)$$

$$U - U_0 = k \left[\frac{x^2}{2} \right]$$

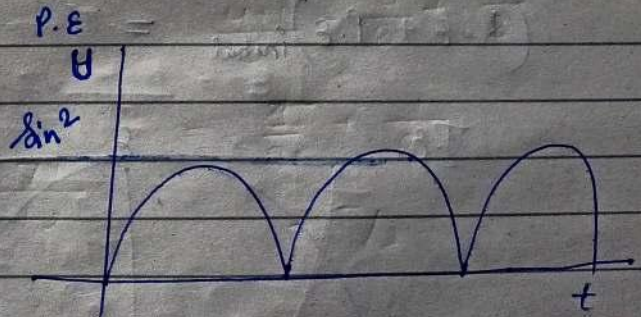
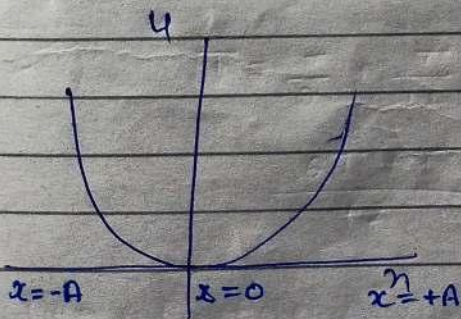
$$U = U_0 + \frac{1}{2} kx^2$$

ref potential at mean

Ques K.E must be zero at Extreme = T
P.E must be zero at mean = f

* If potential energy $U_0 = 0$ at mean

Potential Energy $U = \frac{1}{2} kx^2 = \frac{1}{2} kA^2 \sin^2 \omega t$



Total Energy =

$$T.E = K.E + P.E$$

$$\frac{1}{2}KA^2 \cos^2(\omega t) + \frac{1}{2}KA^2 \sin^2(\omega t)$$

$$T.E = \frac{1}{2}KA^2 [\cos^2 \omega t + \sin^2 \omega t]$$

$$T.E = \frac{1}{2}KA^2$$

At all the time

$$T.E (m.e) = \text{Const}$$

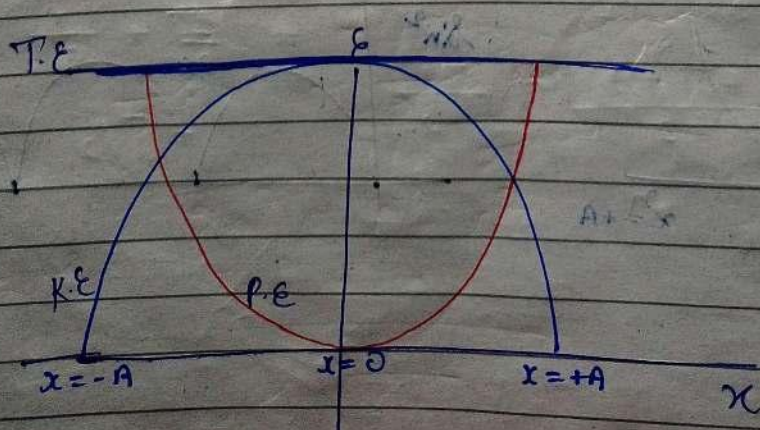
$$T.E = K.E + P.E$$

$$T.E = \frac{1}{2}K(A^2 - x^2) + \frac{1}{2}Kx^2$$

$$T.E = \frac{1}{2}KA^2 - \frac{1}{2}Kx^2 + \frac{1}{2}Kx^2$$

$$T.E = \frac{1}{2}KA^2$$

$$(K.E + P.E)_{\text{initial}} = 3.9$$



Ques 24 The Kinetic energy and P.E of a particle executing S.H.M are equal, when displⁿ in term of amplitude 'A' is,

① $\frac{A}{2}$

$K.E = U$

② $\frac{A}{\sqrt{2}}$ ✓

$K.E + U = T.E = U + U = T.E$

③ $\frac{A\sqrt{2}}{3}$

$\frac{1}{2}kx^2 = \frac{1}{2}kA^2$

④ $A\sqrt{2}$

$x^2 = \frac{A^2}{2} \Rightarrow x = \frac{A}{\sqrt{2}}$

Ques 25 At what displacement the Kinetic Energy is half of the potential Energy?

$K.E = \frac{U}{2}$

$\frac{1}{2}k(A^2 - x^2) = \frac{1}{2}kx^2$

$K.E + U = T.E$

$A^2 - x^2 = x^2$

$\frac{U}{2} + U = \frac{1}{2}kx^2$

$A^2 = \frac{3x^2}{2}$

$\frac{3}{2} \left(\frac{1}{2}kx^2 \right) = \frac{1}{2}kA^2$

$x = \sqrt{\frac{2A^2}{3}}$

$x^2 = \frac{2A^2}{3}$

$x = \sqrt{\frac{2}{3}} A$

$x = \sqrt{\frac{2}{3}} A$

Ques 26 A body is executing SHM with amplitude a and Time Period T . the ratio of Kinetic and P.E when displⁿ from the equilibrium position is half the amplitude

$x = \frac{A}{2}$

① 1:1 $\frac{K.E}{U} = \frac{\frac{1}{2}K(A^2 - x^2)}{\frac{1}{2}Kx^2}$

② 2:1

③ 1:3

④ 3:1 $\frac{A^2 - A^2/4}{\frac{A^2}{4}} = \frac{3A^2/4}{\frac{A^2}{4}} = \frac{3}{1}$

Ques 27 Find ratio of Kinetic & P.E at $x = \frac{x}{4}$

$$K.E = \frac{1}{2}K \left(A^2 - \frac{A^2}{16} \right) = 15 \left(\frac{\frac{1}{2}KA^2}{16} \right)$$

$$U = \frac{1}{2}K \left(\frac{A}{4} \right)^2 = \frac{1}{2}K \frac{A^2}{16}$$

Ques 28 Find position of particle from mean position where P.E is half of the kinetic energy.

$$P.E = \frac{K.E}{2}$$

$$\frac{1}{2}Kx^2 = \frac{1}{2}K(A^2 - x^2)$$

$$2x^2 = A^2 - x^2$$

$$3x^2 = A^2$$

$x = \frac{A}{\sqrt{3}}$

At the time $t=0$, the particle is at its mean position. Then at what time, the particle will have potential energy 50% of its total energy within $t=0$ to $t=T$

$$U = 50\% \cdot T.E$$

$$\frac{1}{2} Kx^2 = \frac{50}{100} \cdot \frac{1}{2} KA^2$$

$$x = \frac{\sqrt{A^2}}{2} = \frac{A}{\sqrt{2}}$$

$$t = \frac{T}{8} \text{ sec}$$

A linear Harmonic Oscillator of force constant $6 \times 10^5 \text{ N/m}$ and amplitude 4 cm, has a total energy 600 J, select the correct statement

Maximum P.E is 600 J

" K.E is 480 J

Minimum P.E is 120 J

All of these

$$K = 6 \times 10^5 \text{ N/m} \quad A = 4 \text{ cm}$$

$$T.E = 600 \text{ J}$$

$$K.E_{\text{max}} = \frac{1}{2} KA^2$$

$$= \frac{1}{2} \cdot 6 \times 10^5 \times \left(\frac{4}{100}\right)^2$$

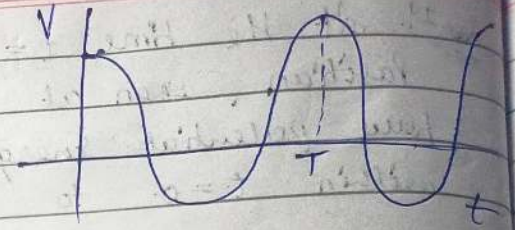
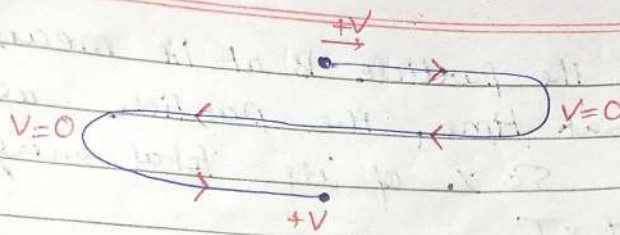
$$= \frac{1}{2} \cdot 6 \times 10^5 \times \frac{16}{10^4}$$

$$U = T.E \quad \cdot \quad K.E + U = T.E$$

$$U_{\text{max}} = 600 \text{ J} \quad 480 + U_{\text{min}} = 600 \text{ J}$$

$$U_{\text{max}} = 600 \text{ J} \quad U_{\text{min}} = 120 \text{ J}$$

$$K.E_{\text{max}} = 480$$

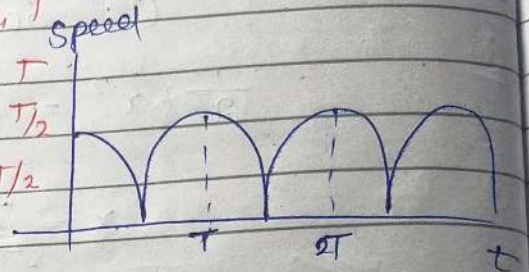


Oscillate its position = f, T

" " Velocity = f, T

" " Speed = $2f, T/2$

" " K.E = $2f, T/2$



Physical Quantity Time period frequency

Position

T

f

Distance

$T/2$

$2f$

Velocity

T

f

Speed

$T/2$

$2f$

Acceleration

T

f

K.E

$T/2$

$2f$

P.E

$T/2$

$2f$

K.E - P.E

$T/2$

$2f$

$|K.E| - |P.E|$

$T/4$

$4f$

M.E

Infinity

Zero

Q11 A loaded vertical spring executes S.H.M with a time period of 4s, the difference b/w the kinetic energy and P.E of this system varies with a period of.

- ① 2s
- ② 1s
- ③ 8s
- ④ 4s

$$t = \frac{T}{2}$$

Time period of S.H.M

Force method - Energy method.

$$F = -Kx$$

$$\therefore a = -\frac{K}{m}x$$

$$a = -\omega^2 x$$

$$F = -\frac{dU}{dx}$$

$$a = \frac{F}{m} = -\frac{1}{m} \left(\frac{dU}{dx} \right)$$

$$\omega = \frac{2\pi}{T}$$

Q12 The P.E of a particle

$$m = 100 \text{ gram} = 0.1 \text{ kg}$$

$$U = 5x(x-4)$$

$$U = 5x^2 - 20x$$

$$F = -\frac{dU}{dx} = -[10x - 20]$$

$$ma = -10x + 20$$

$$a = \frac{-10x}{0.1} + \frac{20}{0.1}$$

$$a = -100x + 200$$

$$\omega^2 = 100$$

$$\frac{2\pi}{T} = \sqrt{100} = \frac{2\pi}{T} = 10 \Rightarrow T = \frac{\pi}{5}$$

Ques P.E of oscillating object is $U = U_0 [1 - \alpha \cos(\alpha x)]$
then find time period of oscillation.

$$U = U_0 (1 - \alpha \cos(\alpha x))$$

$$U = U_0 - \alpha U_0 \cos(\alpha x)$$

$$\frac{dU}{dx} = 0 + \alpha U_0 \sin(\alpha x) \alpha$$

$$\frac{dU}{dx} = \alpha^2 U_0 \sin(\alpha x)$$

$$F = -\frac{dU}{dx}$$

$$F = -\alpha^2 U_0 \sin(\alpha x)$$

$$ma = -\alpha^2 U_0 (\alpha x)$$

cond S.H.M. aplitude small

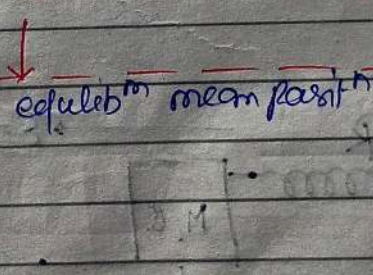
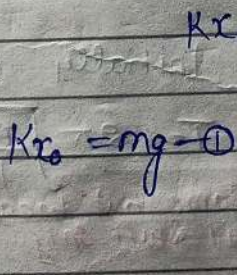
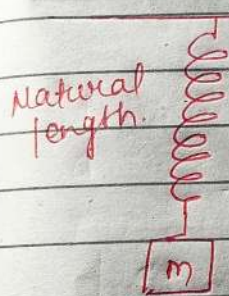
$$a = -\frac{\alpha^3 V_0}{m} x$$

$$\omega^2 = \frac{\alpha^3 V_0}{m}$$

$$\omega = \sqrt{\frac{\alpha^3 V_0}{m}}$$

$$T = 2\pi \sqrt{\frac{m}{\alpha^3 V_0}}$$

Spring mass Oscillation



$$F_{net} = F_s - mg$$

$$ma = k(x+x_0) - mg$$

$$ma = Kx + Kx_0 - mg$$

$$a = \frac{Kx}{m}$$

$$\vec{a} = -\frac{K}{m} \vec{x}$$

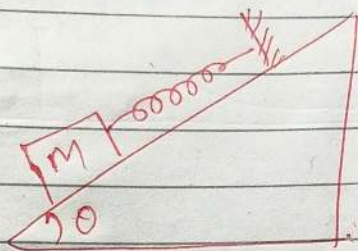
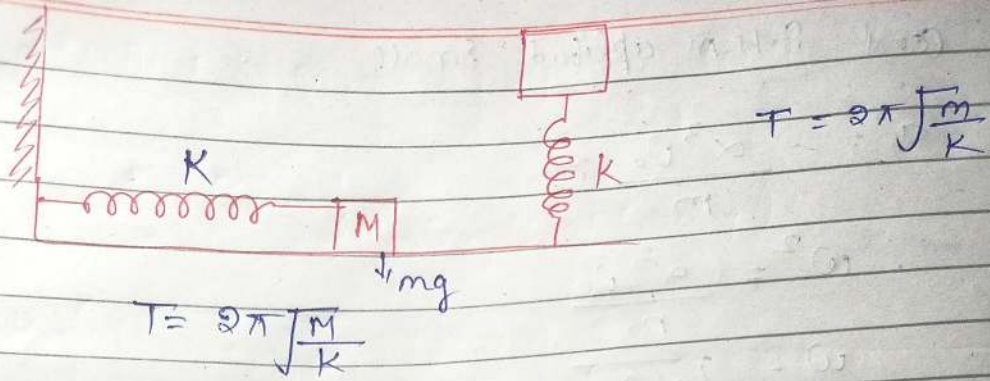
$$\omega = \sqrt{\frac{K}{m}}$$

$$T = 2\pi \sqrt{\frac{m}{K}}$$

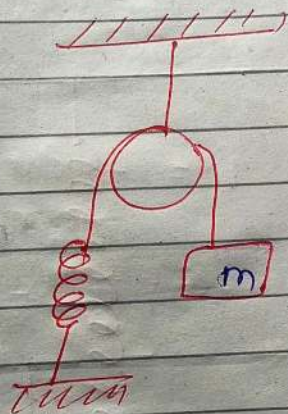
= does not depend on amplitude

= does not depend on g

Variable force $F \propto -x$

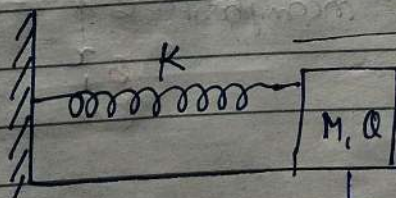


$$T = 2\pi \sqrt{m/k}$$



$$T = 2\pi \sqrt{\frac{M}{K}}$$

Ques



$\epsilon = 0$

Initially $\epsilon = 0$

$$T = 2\pi \sqrt{\frac{M}{K}}$$

Same but mean position will shift only.

max. = M

Charge = Q

Finally Electric field Switch on

① $T = 2\pi \sqrt{\frac{M}{K}}$

② $T < 2\pi \sqrt{\frac{M}{K}}$

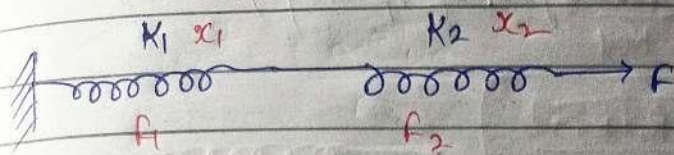
③ $T > 2\pi \sqrt{\frac{M}{K}}$



Combination of Spring

② Parallel Combination

① Series Combination



→ Force same ($F_1 = F_2 = F$)

→ elongation different

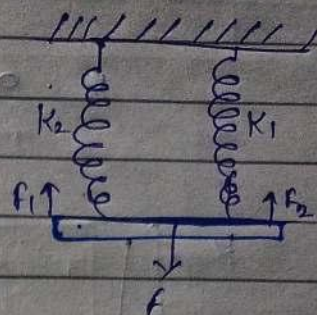


$$x = x_1 + x_2$$

$$\frac{F}{K_{eq}} = \frac{F}{K_1} + \frac{F}{K_2}$$

$$\frac{1}{K_{eq}} = \frac{1}{K_1} + \frac{1}{K_2}$$

$$K_{eq} = \frac{K_1 K_2}{K_1 + K_2}$$



elongation same

force different

$$K_{eq} x = K_1 x + K_2 x$$

$$K_{eq} = K_1 + K_2$$

$$K_1 = K_2$$

$$K_{eq} = 2K$$

IF n - Identical Spring connected in series

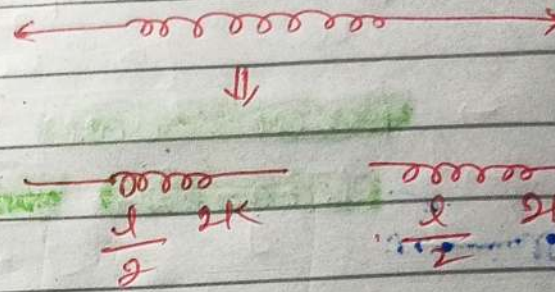
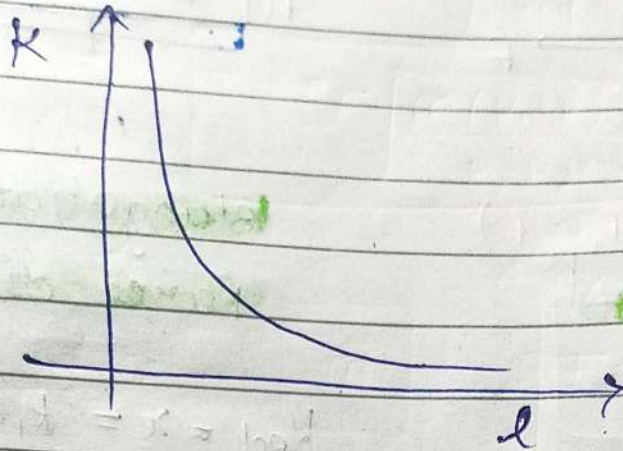
$$K_{eq} = \frac{K}{n}$$

IF n - Identical Spring connected in Parallel

$$K_{eq} = nK$$

Relation b/w length & spring Const

$$K \propto \frac{1}{l \text{ (length of spring)}}$$



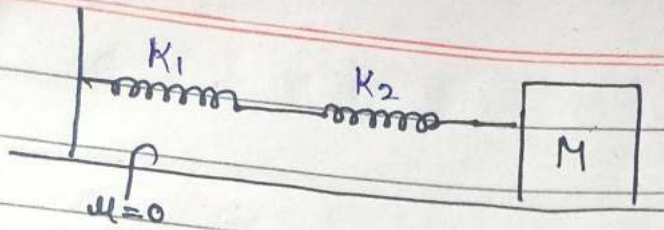
A block of mass m hangs from three springs having same spring constant K . If the mass is displaced downwards, the time period of oscillation will be

$$\sqrt{\frac{m}{3K}}$$

$$\pi \sqrt{\frac{3m}{2K}}$$

$$\pi \sqrt{\frac{2m}{3K}}$$

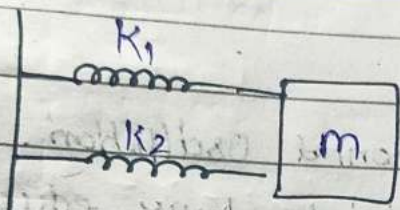
$$\pi \sqrt{\frac{3K}{m}}$$



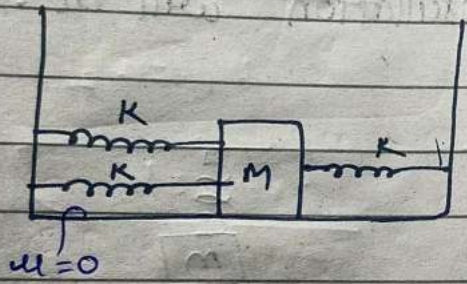
$$K_{eq} = \frac{K_1 K_2}{K_1 + K_2}$$

$$T = 2\pi \sqrt{\frac{m}{K_{eq}}}$$

$$T = 2\pi \sqrt{\frac{m(K_1 + K_2)}{K_1 K_2}}$$

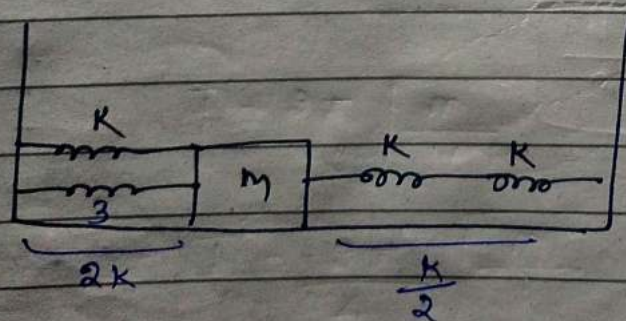


$$T = 2\pi \sqrt{\frac{m}{K_1 + K_2}}$$



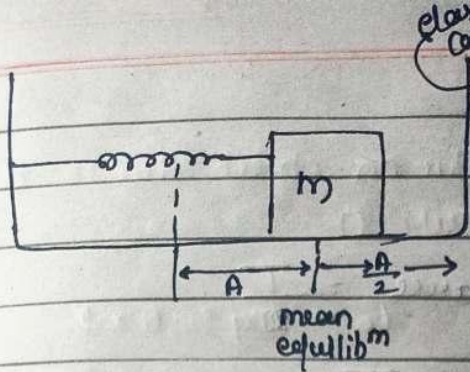
$$K_{eq} = 3K$$

$$T = 2\pi \sqrt{\frac{m}{3K}}$$



$$K_{eq} = 2K + \frac{K}{3} = \frac{7K}{3}$$

$$T = 2\pi \sqrt{\frac{2m}{7K}}$$

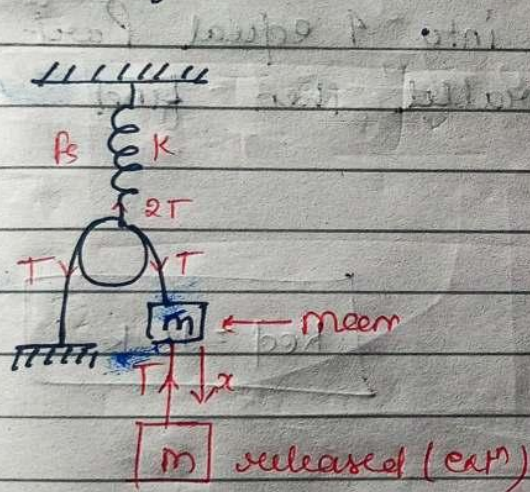


Object is at mean position now it is compressed to a distance A and released as shown in fig. then find time period of periodic motion

$$\frac{T}{2} + \frac{T}{12} + \frac{T}{12} = \frac{T}{2} + \frac{T}{6} = \frac{4T}{6} = \frac{2T}{3} = \frac{2}{3} 2\pi \sqrt{\frac{m}{k}}$$

$$= \frac{4\pi}{3} \sqrt{\frac{m}{k}} \quad \underline{\underline{B}}$$

Object is in equilibrium now displaced x distance downwards then find time



$$RT = F_s = K \left(\frac{x}{2} \right)$$

$$2T = \frac{Kx}{2}$$

$$T = \frac{Kx}{4}$$

Block will accelerate by T

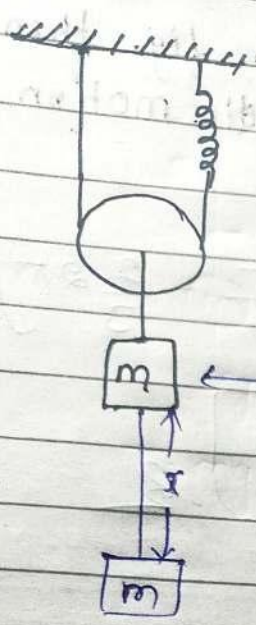
$$T = ma$$

$$ma = \frac{Kx}{4}$$

$$\vec{a} = \frac{K}{4m} \vec{x}$$

$$\omega = \sqrt{\frac{K}{4m}} \quad \therefore T = 2\pi \sqrt{\frac{4m}{K}}$$

Ques Object is in equilibrium.



Spring force $= \frac{T}{2}$

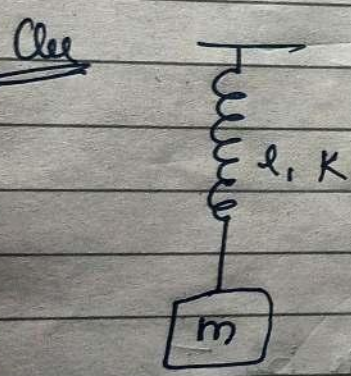
$$k(2x) = \frac{T}{2}$$

$$k(4x) = T$$

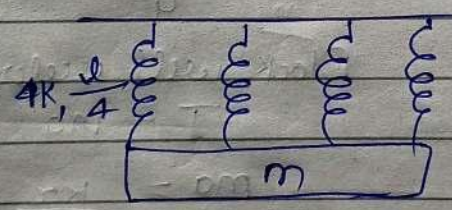
$$4kx = m$$

$$a = \frac{4k}{m} k$$

$$\frac{2\pi}{T} = \omega = \sqrt{\frac{4k}{m}} \Rightarrow T = 2\pi \sqrt{\frac{m}{k}}$$



New Spring is cut into 4 equal Part
Connected in parallel then find
New time period.



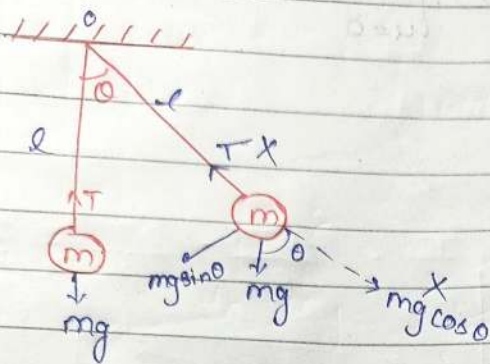
$$K_{eq} = 16K$$

$$T' = 2\pi \sqrt{\frac{m}{16K}}$$

$$T' = \frac{2\pi}{4} \sqrt{\frac{m}{K}}$$

$$T' = \frac{T}{4}$$

Simple pendulum



$T = mg$ (equilibrium position)
mean position

$$T = 2\pi \sqrt{\frac{l}{g}}$$

Torque on object due to $mg \sin \theta$ about 'O'

$$\tau_o = mg \sin \theta \times l$$

$$\tau \propto mg \sin \theta \times l$$

$$\cancel{ml} \propto \cancel{m} g \sin \theta \times \cancel{l}$$

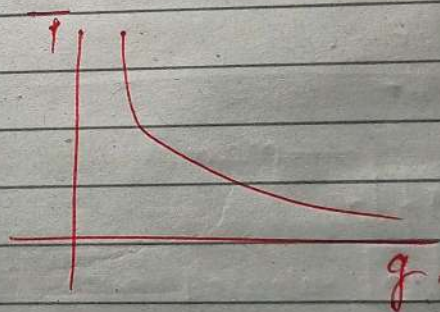
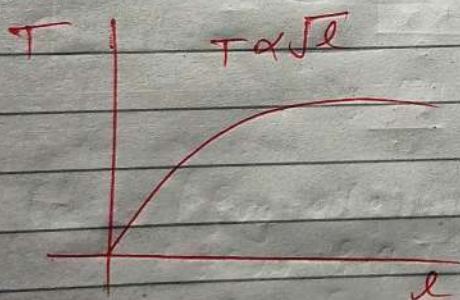
$$\alpha = \frac{g \sin \theta}{l}$$

Condⁿ of S.H.M (θ + small)

$$\alpha = \frac{g}{l} \theta$$

$$\ddot{\alpha} = -\frac{g}{l} \theta \quad \therefore \omega^2 = \frac{g}{l}$$

$$\omega = \sqrt{\frac{g}{l}} = f = \frac{1}{2\pi} \sqrt{g/l}$$



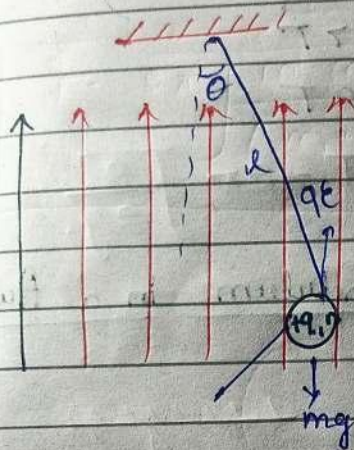
Accelerated Pendulum :- IN LIFT

(i) $T = 2\pi \sqrt{\frac{l}{g+a}}$ (upward acceleration)
 $g_{\text{eff}} = g+a$

(ii) $T = 2\pi \sqrt{\frac{l}{g-a}}$ (downward acceleration)
 $g_{\text{eff}} = g-a$

Simple Pendulum in horizontal accelerated lift

$$T = 2\pi \sqrt{\frac{L}{\sqrt{g^2 + a^2}}} \quad g_{\text{eff}} = \sqrt{g^2 + a^2}$$



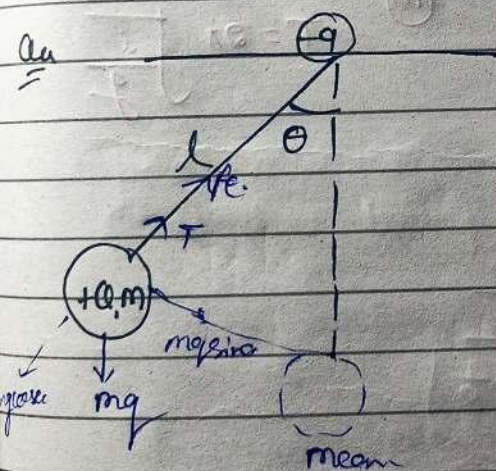
When electric field is zero then
Time period $T = 2\pi \sqrt{\frac{L}{g}}$, And
time period when electric field is
switch on.

(a)

(a) $T' > T$

(b) $T' < T$

(c) $T' = T$

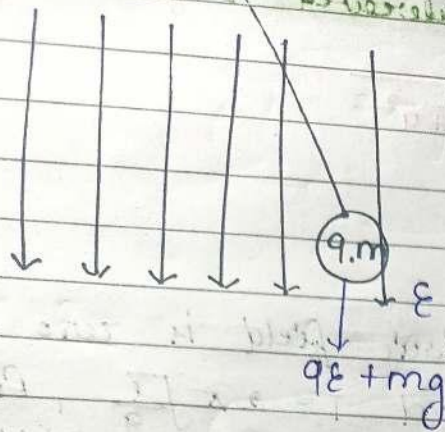


(a) $T = 2\pi \sqrt{L/g}$

(b) $T > 2\pi \sqrt{L/g}$

(c) $T < 2\pi \sqrt{L/g}$

Ques



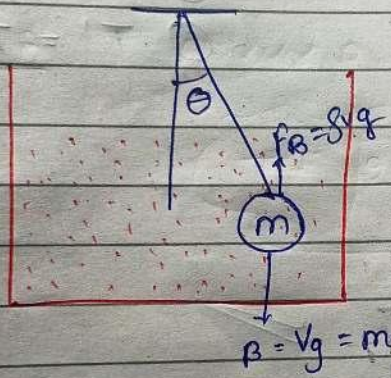
When electric field is zero then time period $T = 2\pi \sqrt{\frac{l}{g}}$. Find time period when electric field is switched on

(a) $T' = T$ (Initial)

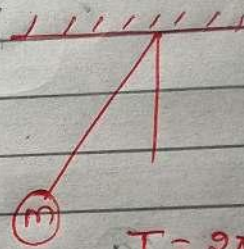
(b) $T' > T$

(c) $T' < T$

Simple Oscillation of simple Pendulum in a fluid



$\sigma > \rho$



$T = 2\pi \sqrt{\frac{l}{g}}$

$F_{net} = (F_{vg} - \sigma(g) \sin \theta)$
 $(\sigma V g - \rho V g) \sin \theta$

$ma = \rho V g \left[1 - \frac{\rho}{\sigma} \right]$

$ma = mg \left(1 - \frac{\rho}{\sigma} \right)$

$a = g \left(1 - \frac{\rho}{\sigma} \right)$

$T' = 2\pi \sqrt{\frac{l}{g \left(1 - \frac{\rho}{\sigma} \right)}}$

$$g = v$$

$$g > v$$

$$v > g$$

$$N = 0$$

float with
cent

$$\frac{v_{in}}{v_{rel}} = \frac{v}{g}$$

$$N' = mg \left(1 - \frac{v}{g} \right)$$

$$mg' = mg \left(1 - \frac{v}{g} \right)$$

$$g = g \left(1 - \frac{v}{g} \right)$$

Ques A simple pendulum with

$$① \quad T/\sqrt{3}$$

$$g = \frac{g}{4}$$

$$② \quad \frac{2T}{\sqrt{3}} \quad \checkmark$$

$$T = 2\pi \sqrt{\frac{l}{g}}$$

$$T' = 2\pi \sqrt{\frac{l}{g \left(1 - \frac{v}{g} \right)}}$$

$$③ \quad \frac{4}{3} T$$

$$T' = 2\pi \sqrt{\frac{l}{g \frac{3}{4}}}$$

$$④ \quad \frac{2}{3} T$$

$$T' = T \sqrt{\frac{4}{3}}$$

$$T' = \frac{2T}{\sqrt{3}}$$

If length of simple pendulum is very large

$$T = 2\pi \sqrt{\frac{l}{g \left(\frac{1}{2} + \frac{1}{2} \right)}}$$

$$T = 2\pi \sqrt{\frac{l}{g}}$$

Very small pendulum

R = Radius of earth

l = length of pendulum

Case-1

$$l \gg R$$

$$T = 2\pi \sqrt{\frac{R}{g}}$$

Case-2

$$l = R$$

$$T = 2\pi \sqrt{\frac{l}{g \frac{2}{R}}}$$

$$= T = 2\pi \sqrt{\frac{R}{2g}}$$

Case-3

$$l \ll R$$

$$T = 2\pi \sqrt{\frac{l}{g}}$$

Ques If effective length of a simple pendulum is equal to radius of earth (R). Time period will be.

① $T = \pi \sqrt{\frac{R}{g}}$

$$T = 2\pi \sqrt{\frac{l}{g \left(\frac{1}{R} + \frac{1}{R} \right)}}$$

② $T = 2\pi \sqrt{\frac{2R}{g}}$

③ $T = 2\pi \sqrt{\frac{R}{g}}$

$$T = 2\pi \sqrt{\frac{R}{2g}}$$

④ $T = 2\pi \sqrt{\frac{R}{2g}}$

boy is swimming in a tank if he stands
the time period will

decrease, then increase

decrease ✓

decrease

remain same

particle is executing simple harmonic motion
period T , then the time period of it
is.

✓

identify the correct definition.

Q. A particle is executing simple harmonic motion with

Second pendulum :-

$$T = 2 \text{ sec}, \quad l = 1 \text{ m}$$

$$T = 2\pi \sqrt{\frac{l}{g}}$$

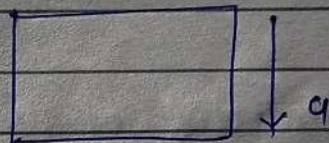
Q. If a second pendulum is moved to a planet where $accl^n$ due to gravity is 4 times, the length of the second's pendulum on the planet should be made.

2 time $g' = 4g$
4 time $T = 2\pi \sqrt{\frac{l}{g}}$
8 time

- ① 1.57 ms^{-1}
- ② 3.12 ms^{-1}
- ③ 2.0 ms^{-1}
- ④ 6.42 ms^{-1}

Q. A Simple pendulum suspended from the ceiling of a stationary lift has period T_0 . When the lift descends at steady speed, the period is T_1 , and when it descends with constant downward accelⁿ the period is T_2 . Which one of the following is true?

- ① $T_0 = T_1 = T_2$
- ② $T_0 = T_1 < T_2$ ✓
- ③ $T_0 = T_1 > T_2$
- ④ $T_0 < T_1 < T_2$



Q. The time period of the oscillation of a simple pendulum is 1 minute. If its length is increased by 44%. Then its new time period of oscillation will be

- ① 96 s
 - ② 88 s
 - ③ 82 s
 - ④ 72 s
- $T = 1 \text{ min}$
 $l_1 = l \text{ (ref)}$
 $l_2 = l + 44\% \cdot l$
 $l_2 = \frac{144}{100} l$

$$T = 2\pi \sqrt{\frac{l}{g}}$$

$$T' = \sqrt{\frac{144}{100}} T$$

$$T' = \frac{12}{10} T = 1.2 T$$

$$\frac{1.2 \times 60 \text{ sec}}{10}$$

$$72 \text{ sec}$$

Ques If the length of a clock pendulum increase by 0.2% due to atmospheric temp. rise then the loss in time of clock per day -

- ① 86.4 s ✓ $T = 2\pi \sqrt{\frac{l}{g}}$
 ② 43.2 s
 ③ 72.5 s
 ④ 32.5 s

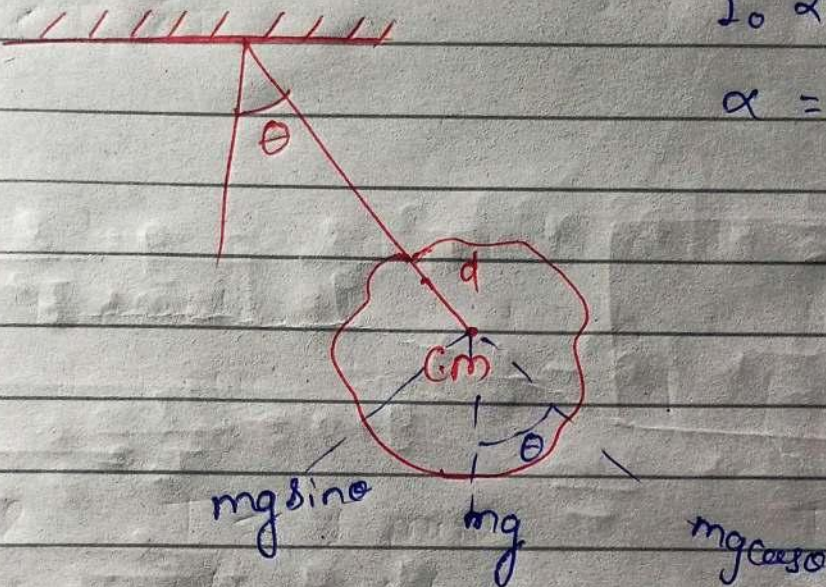
Ans

- ① $\tan^{-1}\left(\frac{g}{a}\right)$ with y axis in +x direction
 $\tan^{-1}\left(\frac{a}{g}\right)$ " " " " -x direction ✓
 $\tan^{-1}\left(\frac{a}{g}\right)$ " " " " +x direction
 $\tan^{-1}\left(\frac{g}{a}\right)$ " " " " -x direction

Ques The time period of oscillation of a second pendulum on the surface of a planet having mass and radius double those of earth is

- ① 4s
 ② 1s
 ③ $\sqrt{2}$ s
 ④ $2\sqrt{2}$ s ✓
- $m_p = 2m_e$
 $R_p = 2R_e$
 $T = 2\pi \sqrt{\frac{l}{g_e}} = 2s$
 $T' = 2\pi \sqrt{\frac{l}{g_p}} = 2\sqrt{2}$
 $g_e = \frac{Gm}{R^2}$
 $g_p = \frac{G(2m)}{4R^2} = \frac{g_e}{2}$

Compound pendulum $\Rightarrow$



$$\tau = mgd \sin \theta$$

$$I_0 \alpha = mgd \sin \theta$$

$$\alpha = \frac{mgd \sin \theta}{I_0} = -\omega^2$$

$$\therefore \omega = \sqrt{\frac{mgd}{I_0}}$$

$$T = 2\pi \sqrt{\frac{I_0}{mgd}}$$

$$d = \text{dist. C.O.M.} \quad I_0 = m a I_0 f$$

f Point of suspension Body from Point
Suspension

Ques A particle is executing SHM and its velocity v is related to its position (x) as $v^2 + ax^2 = b$ where a and b are positive constant. The frequency of oscillation of particle is

① $\frac{1}{2\pi} \sqrt{\frac{b}{a}}$

$$v^2 + ax^2 = b$$

$$v^2 = b - ax^2$$

$$v = \omega \sqrt{A^2 - x^2}$$

$$\omega = \sqrt{a}$$

② $\frac{\sqrt{a}}{2\pi}$ ✓

$$v = \sqrt{b - ax^2}$$

$$= \boxed{f = \frac{\sqrt{a}}{2\pi}}$$

③ $\frac{\sqrt{b}}{2\pi}$

$$v = \sqrt{a \left(\frac{b}{a} - x^2 \right)}$$

④ $\frac{1}{2\pi} \sqrt{\frac{a}{b}}$

$$v = \sqrt{a} \sqrt{\left(\frac{b}{a} - x^2 \right)}$$

Ques A simple pendulum

① $\sqrt{2m\epsilon}$

$$K.E = \frac{1}{2} K (A^2 - x^2)$$

② $\sqrt{\frac{3m\epsilon}{2}}$ ✓

$$K.E = \frac{1}{2} K \left(A^2 - \frac{A^2}{4} \right)$$

③ $2\sqrt{m\epsilon}$

$$K.E = \frac{1}{2} K \frac{3A^2}{4}$$

④ $\sqrt{\frac{2m\epsilon}{3}}$

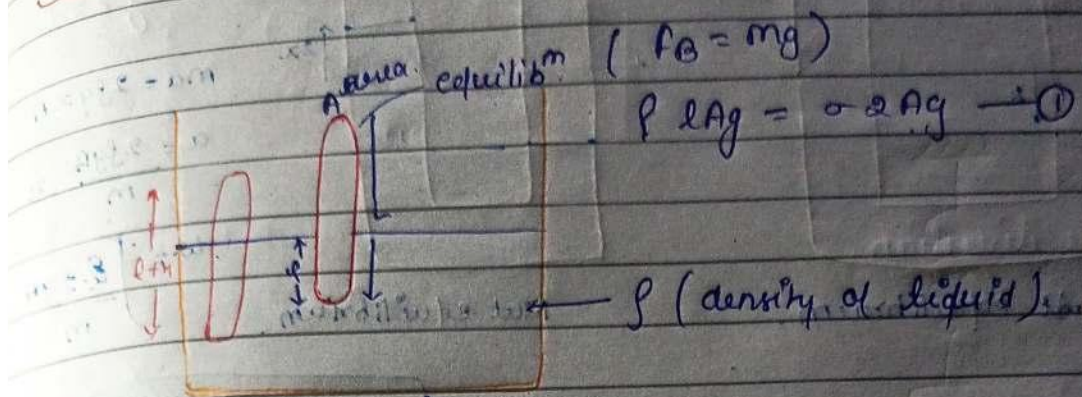
$$K.E = \frac{3\epsilon}{4}$$

$$= \sqrt{2mK.E}$$

$$= \sqrt{2m \times \frac{3\epsilon}{4}}$$

$$= \sqrt{\frac{3m\epsilon}{2}}$$

Oscillation of Solid Cylinder Inside Liquid



$$F_{net} = F_B - mg$$
$$= \rho A (l+x) g - \sigma A g$$

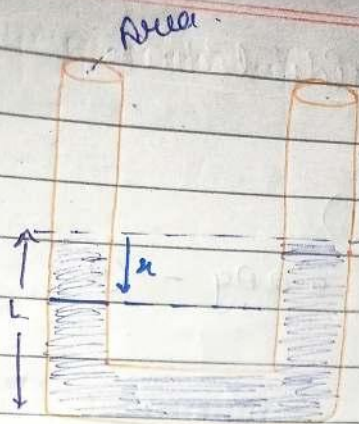
$$ma = \rho A l g + \rho A x g - \sigma A g$$

$$\vec{a} = \frac{\rho A g x}{m} \quad \omega = \sqrt{\frac{\rho A g}{m}}$$

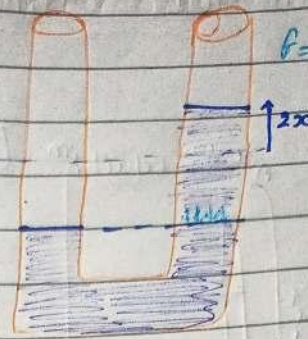
$$T = 2\pi \sqrt{\frac{m}{\rho A g}}$$

$$\therefore T \propto \frac{1}{\sqrt{\rho}}$$

$$\therefore T \propto \frac{1}{\sqrt{\rho}}$$



At equilibrium.



Not equilibrium.

$$F = AP = 2 \rho g x A$$

$$ma = 2 \rho g x A$$

$$a = \frac{2 \rho g A}{m} x$$

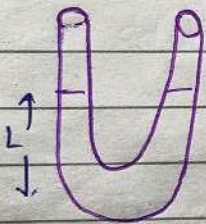
$$\omega = \sqrt{\frac{2 \rho g A}{m}}$$

$$T = 2\pi \sqrt{\frac{m}{2 \rho g A}}$$

mass of liquid.

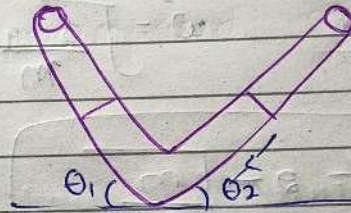
$$T = 2\pi \sqrt{\frac{m}{2 \rho g A}}$$

Ans



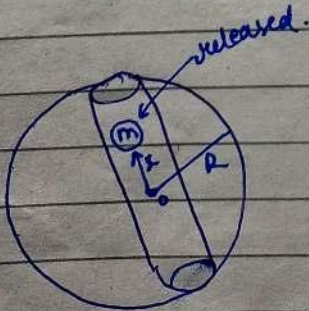
$$T = 2\pi \sqrt{\frac{L}{g}}$$

Ans



$$T = 2\pi \sqrt{\frac{2L}{g(\sin \theta_1 + \sin \theta_2)}}$$

Oscillation of Object in funnel of earth



$$F = mg \Rightarrow \phi a = \phi g \frac{x}{R}$$

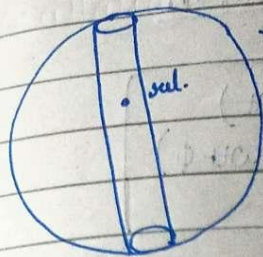
$$g_x = \frac{g x}{R}$$

$$a = \frac{g}{R} x$$

$$\vec{a} = - \frac{g}{R} \vec{x}$$

$$\omega = \sqrt{\frac{g}{R}}$$

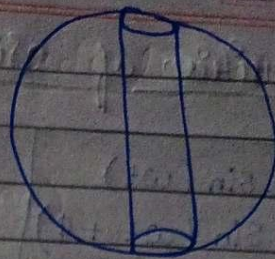
$$T = 2\pi \sqrt{\frac{R}{g}} = 84.6 \text{ sec.}$$



Time period of Oscill

$$T = 2\pi \sqrt{\frac{R}{g}}$$

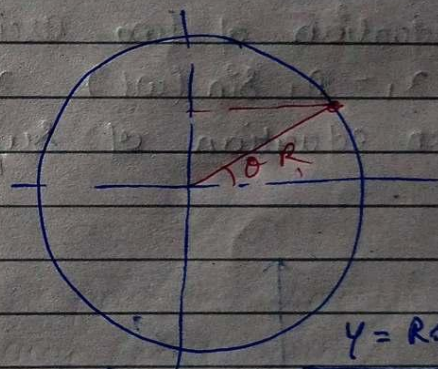
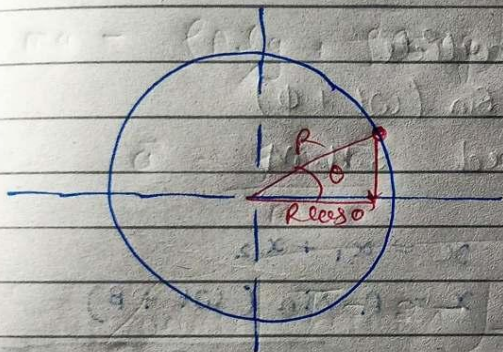
$$84.6 \text{ sec}$$



When two identical object released from same dist from centre then will object will cross the centre.

Ans — Same time

Simple Harmonic as a projection of Circular motion



$$y = R \sin \theta$$

$$y = R \sin(\omega t)$$

Superposition of Simple Harmonic Motion

$$\begin{aligned} x_1 &= A_1 \sin(\omega t) \\ x_2 &= A_2 \sin(\omega t + \phi) \end{aligned}$$

Both are oscillatory in same direction.

$$\begin{aligned} x_1 &= A_1 \sin(\omega t) \\ y_1 &= A_2 \sin(\omega t + \phi) \end{aligned}$$

Both are oscillatory in perpendicular direction.

Superposition of S.H.M $\Rightarrow$

Two Particles Oscillating in Same direction.

Ques Equation of two oscillatory particle
 $x_1 = A_1 \sin(\omega t)$ $x_2 = A_2 \sin(\omega t + \phi)$
 then equation of superimposed S.H.M.

$$x = x_1 + x_2$$

$$x = A \sin(\omega t + \theta)$$

$$A = \sqrt{A_1^2 + A_2^2 + 2A_1A_2 \cos \phi}$$

$$\text{If } A_1 = A_2 = A_0$$

$$A = 2A_0 \cos\left(\frac{\phi}{2}\right)$$

